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Synthetic cooperation in engineered yeast populations

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Cooperative interactions are key to diverse biological phenomena ranging from multicellularity to mutualism. Such diversity makes the ability to create and control cooperation desirable for potential applications in areas as varied as agriculture, pollutant treatment, and medicine. Here we show that persistent cooperation can be engineered by introducing a small set of genetic modifications into previously noninteracting cell populations. Specifically, we report the construction of a synthetic obligatory cooperative system, termed CoSMO (cooperation that is synthetic and mutually obligatory), which consists of a pair of nonmating yeast strains, each supplying an essential metabolite to the other strain. The behavior of the two strains in isolation, however, revealed unintended constraints that restrict cooperation, such as asymmetry in starvation tolerance and delays in nutrient release until near cell death. However, the joint system is shown mathematically and experimentally to be viable over a wide range of initial conditions, with oscillating population ratio settling to a value predicted by nutrient supply and consumption. Unexpectedly, even in the absence of explicitly engineered mechanisms to stabilize cooperation, the cooperative system can consistently develop increased ability to survive reductions in population density. Extending synthetic biology from the design of genetic circuits to the engineering of ecological interactions, CoSMO provides a quantitative system for linking processes at the cellular level to the collective behavior at the system level, as well as a genetically tractable system for studying the evolution of cooperation.

mathematical modeling | mutualism | obligate cooperation | quantitative biology | synthetic ecology

In nature, cooperation emerges under diverse conditions and over varying scales ranging from the physiological, as in the emergence of cell–cell cooperation that facilitates tumor progression (1), to the ecological, as in the evolution of mutualistic interactions between species (2, 3). In laboratory experiments, cooperation among cells of a single population has been shown to arise spontaneously under selective pressures (4), and cooperation between two populations has been attained either through mixing of organisms with natural capacities to cooperate (5, 6) or through evolution from originally parasitic associations (7, 8). All these systems relied on natural processes to establish cooperation. Here, by constructing a synthetic cooperative system, we show that it is possible to create obligatory cooperation, the most stringent form of cooperation, between two previously noninteracting yeast populations.

The existence of natural obligatory cooperative systems (9–13) is puzzling because the viability of both partners relies on cooperation. In certain cases, persistence of the system is achieved through endosymbiosis and vertical transmission of the symbiont (14). However, when both partners are free-living, as in the cases of certain flowers and their pollinators (11, 15, 16) and of metabolically coupled microbes (17–19), it is not clear how reliably viable cooperative communities can form under various initial conditions or how well they can recover from perturbations such as reductions in population size resulting from population bottlenecks. Few studies quantify how features

of a cooperative system are affected by intrinsic constraints stemming from the cooperating partners, such as limited or delayed provision of supplies and imbalanced abundance of partners. This is presumably due to difficulties in measuring beneficial exchanges and population dynamics (2) and in disengaging cooperation from noncooperative interactions, such as competition and inhibition (10, 20) in natural systems.

A simplified synthetic system offers an opportunity to study an elementary ecological interaction in isolation, much like studying a single biochemical reaction outside a cell. Quantitative analysis on the synthetic system can in principle link processes at a finer scale, such as growth, death, and interactions of cooperating cells, to phenomena at a broader scale (21, 22), such as viability outcome and population dynamics of the cooperative system.

Results and Discussion

As the initial step, we genetically modified the yeast *Saccharomyces cerevisiae* to obtain two nonmating strains with different metabolic capabilities (*Methods*) so that they behave essentially as two different species. Specifically, the $R^{\leftarrow A}$ strain, labeled with red-fluorescent protein (DsRed), synthesizes lysine at normal levels but requires adenine to grow; and the $Y^{\leftarrow L}$ strain, labeled with yellow-fluorescent protein (YFP), synthesizes adenine at normal levels but requires lysine to grow. $R^{\leftarrow A}$ and $Y^{\leftarrow L}$ can be propagated in monocultures in the presence of adenine and lysine supplements, respectively. When the two strains were washed free of supplements and subsequently mixed to form a coculture, both strains initially underwent residual growth using stored metabolites (23, 24) but eventually died off (Fig. 1*A*). Thus, although the two populations together have the required enzymes to synthesize both adenine and lysine, their coculture failed to achieve sustained growth.

To create cooperation, we introduced an additional mutation in each strain by replacing the first enzyme in an adenine or a lysine biosynthetic pathway with an overproduction mutant that is no longer sensitive to end-product feedback inhibition (25, 26). Consequently, $R^{\leftarrow A}$ and $Y^{\leftarrow L}$ were respectively transformed into $R^{\leftarrow A}_{\rightarrow L}$, which requires adenine to grow and overproduces lysine, and $Y^{\leftarrow L}_{\rightarrow A}$, which requires lysine to grow and overproduces adenine (Fig. 1*B*).

Despite our goal of creating a simple cooperative system, behavior of individual strains in monocultures reveals unintended constraints that restrict cooperation, such as asymmetric starvation tolerance between the two strains and delayed me-

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The authors declare no conflict of interest.

See Commentary on page 1741.

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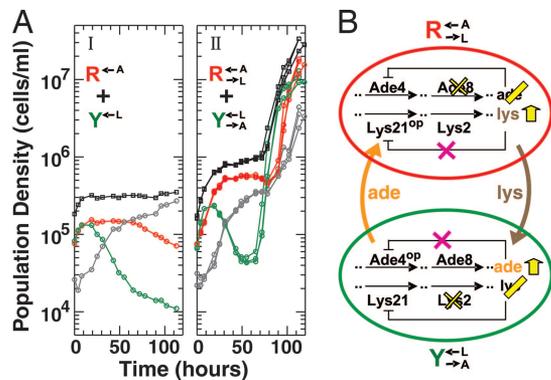


Fig. 1. Rational design of CoSMO. (A) Overproduction of metabolites is required for viable cooperation. At time 0, monocultures of indicated strains grown in synthetic dextrose medium (SD) with the required adenine or lysine supplement (37) were washed free of supplements and mixed. Plots show population dynamics of fluorescent live R (red), fluorescent live Y (green), nonfluorescent dead (gray), and total (black) cells of the coculture as measured by flow cytometry (Methods). (II) Data from three replicate cultures are superimposed. (B) The “wiring” diagram of CoSMO. CoSMO consists of two yeast strains: $R_{\leftrightarrow A}^{\leftarrow}$, which lacks Ade8 enzyme and harbors Lys21^{OP} enzyme, and $Y_{\leftrightarrow A}^{\leftarrow}$, which lacks Lys2 enzyme and harbors Ade4^{OP} enzyme. Cells lacking Ade8 (Lys2) cannot synthesize adenine (lysine) and therefore require intake (\leftarrow) of the corresponding metabolite. Ade4^{OP} and Lys21^{OP} are no longer sensitive to end-product feed-back inhibition and consequently overproduce (^{OP}) the corresponding metabolite that is eventually released (\rightarrow) into the medium (25, 26). Crosses represent genetic inactivation; yellow bars and arrows represent losses and gains in metabolite synthesis, respectively.

tabolite release until near cell death. After washout of the essential adenine or lysine supplement, each strain initially underwent residual growth using stored metabolites (23, 24) until time $T_I \approx 10$ h (Fig. 2A). Immediately afterward, $Y_{\leftrightarrow A}^{\leftarrow}$ cells entered the death phase characterized by a decrease in the number of live cells (Fig. 2A, green stars) and an increase in the number of dead cells (Fig. 2B, gray squares). $R_{\leftrightarrow A}^{\leftarrow}$ cells, in contrast, did not enter death phase until time $T_R, \approx 70$ h (Fig. 2A red stars and Fig. 2B gray circles). The release of the overproduced metabolites into the medium was associated with cell death (Fig. 2B). Consequently, the onset of lysine release by $R_{\leftrightarrow A}^{\leftarrow}$ was significantly delayed until time T_R , when the majority of $Y_{\leftrightarrow A}^{\leftarrow}$ population already lost viability (Fig. 2B).

Despite the presence of strong constraints, cooperation can exist between $R_{\leftrightarrow L}^{\leftarrow}$ and $Y_{\leftrightarrow A}^{\leftarrow}$, as verified through the viability of their cocultures. Coculture viability is defined here as the ability to attain saturation density ($\approx 5 \times 10^7$ total cells per ml) in the absence of adenine and lysine supplements. We found that cocultures initiated at low density ($\approx 10^5$ total cells per ml) can be viable (Fig. 1AII) and that viability of cooperation requires both adenine- and lysine-overproduction mutations [supporting information (SI) Fig. 6]. Together, $R_{\leftrightarrow L}^{\leftarrow}$ and $Y_{\leftrightarrow A}^{\leftarrow}$ form a cooperative system termed CoSMO (cooperation that is synthetic and mutually obligatory), which mimics two-species obligate mutualistic systems in which cooperation is essential for the survival of both species (11, 14, 17, 19, 27, 28).

We used the individual characteristics of the two strains to compute viability conditions for CoSMO (Fig. 2C and Appendix). A fundamental requirement for system viability is that the supply of metabolites has to be sufficiently high to sustain net growth of both partners. In mathematical terms, this condition is expressed as $A_s L_s / A_c L_c > 1$ (Appendix, supply-consumption requirement), where A_s (L_s) is the total amount of adenine (lysine) supplied per $Y_{\leftrightarrow A}^{\leftarrow}$ ($R_{\leftrightarrow L}^{\leftarrow}$) cell until its death, and A_c (L_c) is the amount of adenine (lysine) consumed to make a new $R_{\leftrightarrow L}^{\leftarrow}$ ($Y_{\leftrightarrow A}^{\leftarrow}$) cell. For CoSMO, experimentally measured values (SI Table 1) lead to $A_s L_s / A_c L_c \approx$

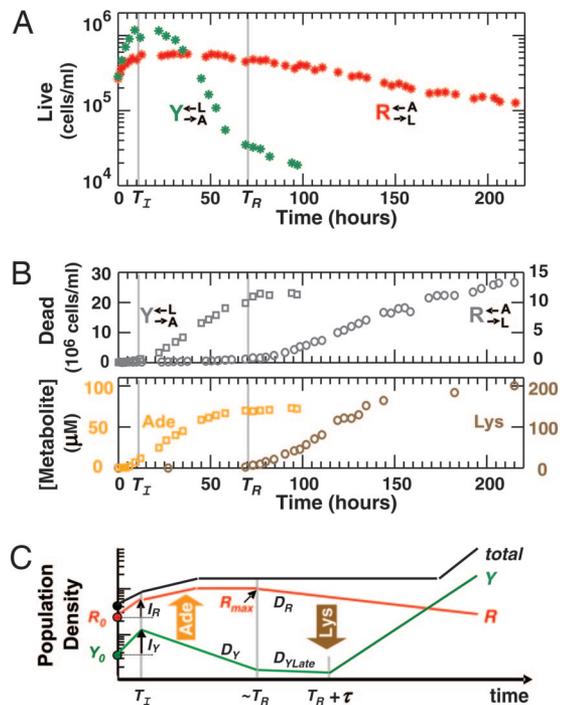


Fig. 2. Characterization of individual strains in monocultures and deduction of CoSMO growth pattern. (A and B) Asymmetry in starvation tolerance between two strains and delayed metabolite release. At time 0, monocultures of the two strains grown in the presence of the required supplement were washed free of the supplement. (A) Live population density over time for an initial population density of $\approx 3 \times 10^5$ cells per ml. (B) Dead population density (Upper) and the concentration of lysine or adenine released into the medium over time (Lower) as measured by a bioassay (Methods) for an initial population density of $\approx 6 \times 10^6$ cells per ml. The left and right scales are for experiments on $Y_{\leftrightarrow A}^{\leftarrow}$ (squares) and $R_{\leftrightarrow L}^{\leftarrow}$ (circles), respectively. Gray vertical lines mark the time T_I when residual growth ends and the time T_R when $R_{\leftrightarrow L}^{\leftarrow}$ enters death phase and releases lysine. (C) A schematic diagram of the initial stage of CoSMO growth deduced from A and B. R and Y denote live population densities of $R_{\leftrightarrow L}^{\leftarrow}$ and $Y_{\leftrightarrow A}^{\leftarrow}$, respectively. Their initial values R_0 and Y_0 increase l_R - and l_Y -fold, respectively, during residual growth until time T_I . After T_I , adenine released from dying $Y_{\leftrightarrow A}^{\leftarrow}$ enables growth of $R_{\leftrightarrow L}^{\leftarrow}$. By time $\approx T_{R_i}$, most of the $Y_{\leftrightarrow A}^{\leftarrow}$ population has died and R is at a local maximum R_{max} . Lysine is subsequently released from dying $R_{\leftrightarrow L}^{\leftarrow}$, and at some time τ after T_R , results in an increase in Y under conditions that permit CoSMO viability. The death rate for $R_{\leftrightarrow L}^{\leftarrow}$ after T_R is D_R , and for $Y_{\leftrightarrow A}^{\leftarrow}$ is D_Y from T_I to T_R and D_{YLate} from T_R onward. The total cell density, which is the sum of R , Y , and dead populations, consequently takes on a pattern of “rise-plateau-rise,” with each rise resulting from net growth of at least one partner.

22, implying that CoSMO significantly exceeds this fundamental supply-consumption requirement.

However, the system can fail to be viable if a released metabolite is too dilute and therefore its uptake rate is too slow to keep its consumer alive, or if any one strain goes extinct before its partner strain has a chance to release a substantial amount of metabolite. These two failure modes lead to constraints on the initial cell densities (Appendix, minimum initial cell density requirement) and initial cell numbers (Appendix, minimum initial cell number requirement). The two requirements can be combined to define the viability and inviability domains of CoSMO as a function of the initial densities of the two strains at a given volume. The two domains can be represented in a phase diagram (Fig. 3), which collapses multiple quantitative properties of the component strains into a concise predictive description of CoSMO system behavior.

For initial conditions well within the calculated inviable domain (Fig. 3, broken circles), replicate CoSMO cultures are

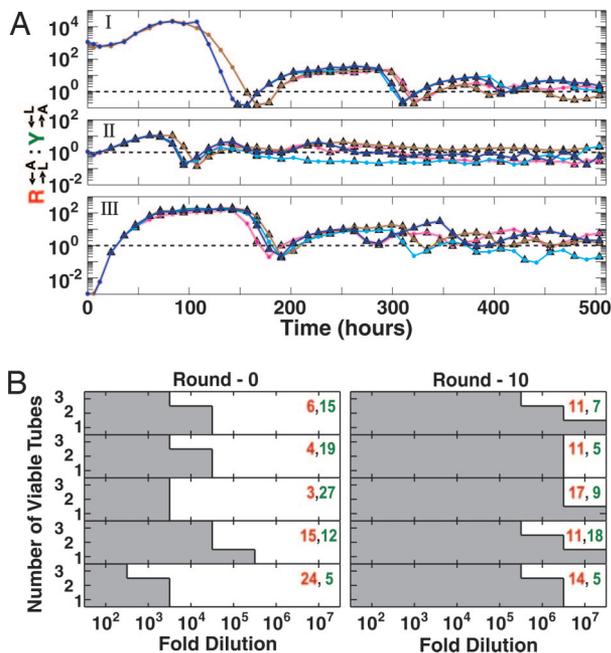


Fig. 5. Long-term changes in CoSMO. (A) Stabilization of partner ratios. At time 0, duplicate CoSMO cultures (brown and blue) were initiated at OD_{600} of 0.01 (4.7×10^5 total cells per ml) and $R_{\rightarrow A}^{-A}:Y_{\rightarrow L}^{-L}$ ratios of 10^3 (I), 1 (II), and 10^{-3} (III). When OD_{600} exceeded the set point of 0.06 for the first time, two 3-ml samples were taken from each culture (brown and magenta from the brown; blue and cyan from the blue), and thereafter diluted once per day (magenta and cyan) or twice per day (brown and blue) to the set point. A low set point was chosen so that nutrients other than adenine and lysine were not limiting. Plots show $R_{\rightarrow A}^{-A}:Y_{\rightarrow L}^{-L}$ ratios over time, with triangles marking points of dilution. (B) Increased ability to survive reductions in population density. Five 2.6-ml CoSMO cultures, initiated at different partner ratios, were grown to near-saturation and used as Round-0 cultures for five independent series. After 10 rounds of dilution and regrowth in 2.6 ml, a near-saturation Round-10 culture was obtained for each series. Each row corresponds to a particular series and depicts the number of tubes (of three) that were viable at indicated dilutions for Round-0 (Left) and Round-10 (Right) cultures. Population densities of $R_{\rightarrow A}^{-A}$ (red) and $Y_{\rightarrow L}^{-L}$ (green) in million cells per ml for Round-0 and Round-10 cultures are shown in the *Inset*.

population bottlenecks, a commonly occurring perturbation. Five CoSMO cultures were initiated, grown to near-saturation (Round 0), and subjected to 10 rounds of dilution-and-regrowth, ending in Round-10 cultures (protocol illustration in SI Fig. 8). The population density of both Round-0 and Round-10 cultures was on the order of 10^7 total cells per ml. The Round-0 cultures typically tolerated 10^3 - to 10^4 -fold dilution (Fig. 5B Left), and therefore a total population density on the order of 10^3 to 10^4 cells per ml was required for the viability of a diluted CoSMO culture. In contrast, the Round-10 cultures typically tolerated 10^5 - to 10^6 -fold dilution (Fig. 5B Right), and therefore a total population density on the order of 10^1 to 10^2 cells per ml was sufficient for viability. Thus, although the initial requirements for viable cooperation can be accurately predicted from properties of components (Fig. 3), the density requirement underwent 100-fold relaxation over a relatively short period (≈ 70 generations). This phenomenon may result from changes in one or both strains that aid the survival of the strain itself (e.g., through increased starvation tolerance) or the survival of its partner (e.g., through increased overproduction or expedited release of metabolites). Unlike natural systems in which partner coevolution has rendered the evolutionary history of cooperation difficult to retrace (11), multiple CoSMO cultures can be initiated and their evolutionary trajectories compared. Uncovering the nature of these changes will elucidate the adaptation pathways of cooperation and the diversity in adaptive strategies (6).

Our results show that persistent cooperation between two populations can be created *de novo* through a small set of targeted genetic modifications. In fact, each population is essentially only one mutation step away from being a cooperator. Despite its artificial origin, CoSMO closely mimics aspects of naturally occurring cooperative systems such as exchange of essential nutrients between partners (14, 19, 28), death of a fraction of one partner population to support the reproduction of the other partner (11, 27), and delayed reward for a particular investment (11, 27). Even with obstacles such as severe delays in nutrient release, significant asymmetry in partners' starvation tolerance, and skewed population ratios resulting from intrinsic dynamics, the range of conditions permissible for cooperation is wide, consistent with the diversity observed in naturally occurring cooperative systems (2, 3). Although the interplay between cooperative organisms in natural systems must be far richer and deeper, we show that even in a simplified synthetic cooperative system, novel properties such as increased ability to stay alive could emerge. Future work is required to analyze the viability requirements, the population dynamics, and the evolution of CoSMO when challenged by "cheater" strains such as $Y_{\rightarrow L}^{-L}$ and $R_{\rightarrow A}^{-A}$, which consume metabolites and release none. This would allow a quantitative assessment of a key question in the evolution of cooperation: the persistence of cooperation in the face of individuals that reap benefits without paying the cost of cooperation.

Our work highlights the importance of quantitatively linking processes on finer scales to system behavior at larger scales and underscores the challenges in predicting the behavior of an adapting biological system.

Methods

Construction of CoSMO Components. Yeast strains of desired genotypes were obtained through genetic crosses. The complete genotype for WY811 ($R_{\rightarrow A}^{-A}$) is *MATa ste3Δ::kanMX4 ade8Δ0 LYS21^{op} trp1-289::pRS404(TRP)-ADHp-DsRed.T4* and that for WY833 ($Y_{\rightarrow L}^{-L}$) is *MATa ste3Δ::kanMX4 ADE4^{op} lys2Δ0 trp1-289::pRS404(TRP)-ADHp-venus-YFP*.

lys2Δ and *ade8Δ* mutations were derived from BY4743 (Euroscarf Y20000) (31) and SY9913 (32), respectively. Yeast cells of the same mating type do not mate. *ste3Δ::KanMX4* (Euroscarf Y05028) cells lack Ste3, the receptor for α -mating factor (33). Thus, in the rare occasion where a cell of *MATa ste3Δ* genotype switches mating type to *MAT α ste3Δ*, it still cannot mate.

ADE4^{op} mutant is the *PUR6* allele of *ADE4* (26). *LYS21^{op}* was isolated in an MNNG (1-methyl-3-nitro-1-nitrosoguanidine, Sigma-Aldrich, St. Louis, MO) mutagenesis screen as a mutation that was resistant to the lysine analog thialysine (L-4-thialysine hydrochloride, Sigma-Aldrich) and that also cross-fed *lysΔ* cells (34). One lysine-releasing mutation was dominant, showed tight linkage to *LYS21* (20/20 tetrads), and was therefore assigned *LYS21^{op}*. Both *ADE4^{op}* and *LYS21^{op}* mutations were backcrossed into the S288C background five times.

To introduce fluorescent protein markers, WSB37 and WSB41 were constructed after ligating three DNA fragments: the *TRP1*-integrating plasmid pRS404 (American Type Culture Collection, Manassas, VA) digested with SacI and XhoI, a SacI-HindIII fragment harboring the ADH promoter from pKW431 (35), and a HindIII-XhoI PCR fragment containing either Venus-YFP amplified from pDH6 (<http://depts.washington.edu/~yeastrc/>) or RGS-His6-DsRed.T4 amplified from pQE81-L-DsRed.T4 (36). The resulting plasmids were linearized with XbaI and transformed into a yeast strain harboring *trp1-289*. Among *TRP*⁺ transformants, a stable integrant was selected such that all its progeny cells expressed the expected

fluorescent protein even when grown in nonselective media containing tryptophane.

Measurement of Metabolite Concentration Using a Bioassay. A series of SD media (37) supplemented with various amounts of metabolite adenine (lysine) and inoculated with a test strain auxotrophic for adenine (lysine) were grown to saturation (≈ 20 h). A linear regression of saturation OD₆₀₀ values against concentrations of the metabolite was performed (correlation coefficient >0.99). To measure the metabolite concentration in a culture, the culture was filtered through a 0.2- μm filter, and the supernatant was supplemented with 1/10 volume of $10\times$ SD and inoculated with the appropriate test strain. The metabolite concentration was obtained from the saturation OD₆₀₀ value through interpolation.

Measurement of Population Dynamics Using Flowing Cytometry. For every round of measurement on FACS Calibur (with 488-nm and 633-nm lasers; BD Biosciences, Franklin Lakes, NJ), the flow rate k of the instrument ($\mu\text{l}/\text{sec}$) was determined using a dilution series of a bead stock. Specifically, the concentration of a 6- μm bead stock ($\approx 2 \times 10^6$ per ml; Duke Scientific, Fremont, CA, catalog no. 35-2) was measured using a hemacytometer. The bead stock was diluted 25-, 10-, 5-, and 2.5-fold to a standard 0.5-ml series of bead samples and processed by Calibur for 65 sec. The cumulative event counts at 5.2, 10.0, 15.2, 20.0, 25.2, and 30.0 sec were plotted against time, and the event rate (events per sec) for each bead sample was deduced from the slope. Event rates (events per sec) were plotted against bead densities (beads per μl) for the standard series, and the linear regression line was forced through the origin. The slope k was the flow rate of Calibur ($\mu\text{l}/\text{sec}$). The correlation coefficients of all linear regressions were >0.999 .

To measure the population composition of a culture, a sample was diluted into H₂O to OD₆₀₀ ≈ 0.01 and briefly sonicated. S , the event rate of the sample (events per sec), was determined as described above for bead samples. The total cell density is S/k (events per μl). Clusters of DsRed-positive, YFP-positive, and dark cells were clearly segregated (SI Fig. 9), and the percentages of each cluster were calculated using FlowJo software (TreeStar, Ashland, OR). Dark cells accumulated during starvation and were considered dead because $>99\%$ (sample size $>5,000$) had lost colony-forming ability in a FACS analysis. Fluorescent cells are considered alive because all of them retain the ability to exclude the nucleic acid dye propidium iodide (sample size >150).

Calculation of the Steady-State Population Ratio. When a finite nonzero steady state ratio is achieved, $R_{\rightarrow L}^{\leftarrow A}$ and $Y_{\rightarrow A}^{\leftarrow L}$ grow with the same rate \bar{G} . Furthermore, let \bar{D}_R and \bar{D}_Y represent the death rates of $R_{\rightarrow L}^{\leftarrow A}$ and $Y_{\rightarrow A}^{\leftarrow L}$ at this stage, respectively.

Because $\Delta\bar{R}/\Delta R = \bar{D}_R R \Delta t / \bar{G} R \Delta t$ and $\Delta\bar{Y}/\Delta Y = \bar{D}_Y Y \Delta t / \bar{G} Y \Delta t$, Eq. 1 in Appendix becomes

$$\Delta R = \frac{\bar{D}_Y}{\bar{G}} \Delta Y \frac{A_s}{A_c} - \frac{\bar{D}_R}{\bar{G}} \Delta R \text{ and } \Delta Y = \frac{\bar{D}_R}{\bar{G}} \Delta R \frac{L_s}{L_c} - \frac{\bar{D}_Y}{\bar{G}} \Delta Y.$$

Solving for $\Delta R/\Delta Y$ after replacing \bar{G} , we obtain

$$\frac{\Delta R}{\Delta Y} = \frac{L_c}{2L_s} \left[\frac{\bar{D}_Y}{\bar{D}_R} - 1 + \sqrt{4 \frac{\bar{D}_Y A_s L_s}{\bar{D}_R A_c L_c} + \left(\frac{\bar{D}_Y}{\bar{D}_R} - 1 \right)^2} \right].$$

If we assume $\bar{D}_Y/\bar{D}_R = D_{Y\text{late}}/D_R$, then $\Delta R/\Delta Y \approx 1$ for CoSMO (SI Table 1). $R/Y = (R_0 + \Delta R)/(Y_0 + \Delta Y)$ tends to $\Delta R/\Delta Y$ when t is large because R_0 and Y_0 are small compared with ΔR and ΔY . Therefore, R/Y is on the order of 1 for CoSMO. In CoSMO, $\bar{D}_Y/\bar{D}_R - 1$ is small compared with $(4\bar{D}_Y A_s L_s / \bar{D}_R A_c L_c)^{1/2}$, in

which case R/Y can be simplified to $(\bar{D}_Y A_s L_s / \bar{D}_R A_c L_c)^{1/2}$, a function of adenine and lysine supply rates ($\bar{D}_Y A_s$ and $\bar{D}_R L_s$) and consumption (A_c and L_c).

Appendix: Three Requirements for CoSMO Viability

Supply-Consumption Requirement. Supply of metabolites must be sufficiently high to sustain net growth of both components. Let A_s (L_s) be the total amount of adenine (lysine) supplied per $Y_{\rightarrow A}^{\leftarrow L}$ ($R_{\rightarrow L}^{\leftarrow A}$) cell until its death, and let A_c (L_c) be the amount of adenine (lysine) consumed to make a new $R_{\rightarrow L}^{\leftarrow A}$ ($Y_{\rightarrow A}^{\leftarrow L}$) cell. Assuming that all released metabolites are completely consumed, changes (Δ) in population densities of live $R_{\rightarrow L}^{\leftarrow A}$ and $Y_{\rightarrow A}^{\leftarrow L}$, denoted R and Y , and of the corresponding dead cells, denoted \bar{R} and \bar{Y} , are related through

$$\Delta R = \Delta\bar{Y} \frac{A_s}{A_c} - \Delta\bar{R} \text{ and } \Delta Y = \Delta\bar{R} \frac{L_s}{L_c} - \Delta\bar{Y}. \quad [1]$$

Positive growth of both components requires $\Delta\bar{Y}(A_s/A_c) > \Delta\bar{R}$ and $\Delta\bar{R}(L_s/L_c) > \Delta\bar{Y}$, which leads to $A_s L_s / A_c L_c > 1$. This condition is analogous to those derived in mathematical models of obligate mutually cross-feeding systems in chemostats at steady state (38).

Minimum Initial Cell-Density Requirement. The growth rate of $Y_{\rightarrow A}^{\leftarrow L}$, G_Y , must exceed the death rate $D_{Y\text{late}}$ at a finite time τ after the initiation of lysine release from dying $R_{\rightarrow L}^{\leftarrow A}$ at time $\approx T_R$ (Fig. 2C). If each $Y_{\rightarrow A}^{\leftarrow L}$ cell uptakes lysine at concentration L in the medium following Michaelis-Menten kinetics with half-saturation constant K_{mL} and maximum rate $V_{\text{max}L}$, and produces a new cell after acquiring a quantity L_c of lysine, we obtain

$$D_{Y\text{late}} < G_Y = \frac{1}{L_c} \frac{V_{\text{max}L}}{K_{mL} + L} L \approx \frac{1}{L_c} \frac{V_{\text{max}L}}{K_{mL}} L. \quad [2]$$

Note that measured L is small compared with K_{mL} . L is given by

$$L = R_{\text{max}} (1 - e^{-D_R \tau}) L_s, \quad [3]$$

where R_{max} is the population density of $R_{\rightarrow L}^{\leftarrow A}$ at time T_R , and $(1 - e^{-D_R \tau})$ is the fraction of $R_{\rightarrow L}^{\leftarrow A}$ cells that have died from time T_R to $T_R + \tau$. R_{max} is related to R_0 and Y_0 , the initial population densities of the two partners, through

$$R_{\text{max}} \approx I_R R_0 + I_Y Y_0 \frac{A_s}{A_c}, \quad [4]$$

accounting for increase in R resulting first from I_R -fold residual growth from R_0 and then from adenine released on the death of almost the entire $Y_{\rightarrow A}^{\leftarrow L}$ population, which has undergone I_Y -fold residual growth from Y_0 . From inequality 2, Eq. 3, and the measured parameters (SI Table 1), we obtain the minimal R_{max} required for CoSMO viability as

$$R_{\text{max}}^* = \frac{D_{Y\text{late}} K_{mL} L_c}{V_{\text{max}L} L_s} \approx 6 \times 10^4 \text{ cells per ml}. \quad [5]$$

Minimum Initial Cell-Number Requirement. For a coculture of volume V , the initial number of $R_{\rightarrow L}^{\leftarrow A}$ cells must be at least 1

$$R_0 V \geq 1. \quad [6]$$

In addition, there must be at least one $Y_{\rightarrow A}^{\leftarrow L}$ cell alive at time $T_R + \tau$

$$I_Y Y_0 V e^{-D_Y(T_R - T_i) - D_{Y\text{late}} \times \tau} \geq 1. \quad [7]$$

From inequalities 2 and 7 and Eqs 3–5, we obtain the condition

$$Y_0V > \frac{e^{(T_R - T_I)D_Y}}{I_Y} \left(1 - \frac{R_{\max}^*}{R_{\max}} \right)^{\frac{-D_Y L_{\text{late}}}{D_R}}$$

$$\approx \frac{e^{(T_R - T_I)D_Y}}{I_Y} \left(1 - \frac{R_{\max}^*}{I_R R_0 + I_Y Y_0 A_s / A_c} \right)^{\frac{-D_Y L_{\text{late}}}{D_R}} \quad [8]$$

The minimum initial number of $Y_{\rightarrow A}^{\leftarrow L}$ cells required for CoSMO viability is obtained after setting R_0 in inequality 8 to the saturation density 5×10^7 cells per ml:

$$Y_0V \geq 9. \quad [8a]$$

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