

DICTIONARY BASED HYPERSPECTRAL IMAGE RETRIEVAL

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Abstract: The normalized information distance (NID) is an universal metric distance based on Kolmogorov complexity. However, NID is not computable in a Turing sense. The normalized compression distance (NCD) is a computable distance that approximates NID by using normal compressors. NCD is a parameter-free distance that compares two signals by their lengths after separate compression relative to the length of the signal resulting from their concatenation after compression. The use of NCD for image retrieval over large image databases is difficult due to the computational cost of compressing the query image concatenated with every image in the database. The use of dictionaries extracted by dictionary-based compressors, such as the LZW compression algorithm, has been proposed to overcome this problem. Here we propose a Content-Based Image Retrieval system based on such dictionaries for the mining of hyperspectral databases. We compare results using the Normalized Dictionary Distance (NDD) and the Fast Dictionary Distance (FDD) against the NCD over different datasets of hyperspectral images. Results validate the applicability of dictionaries for hyperspectral image retrieval.

1 INTRODUCTION

Kolmogorov complexity lies in the core of *algorithmic information theory* (Chaitin, 2004; Solomonoff, 2009) that focuses on the information of individual signals, an approach completely different to classical Shannon's probabilistic approach to information theory (Shannon, 2001). The normalized information distance (NID) (Bennett et al., 1998) is an universal metric distance based on Kolmogorov complexity (Li and Vitanyi, 1997). However, NID is stated in terms of Kolmogorov complexity which is uncomputable in a Turing sense. The normalized compression distance (NCD) (Li et al., 2004) is a computable distance that approximates NID by using normal compressors. There has been an increasing interest in using NCD for pattern recognition (Watanabe et al., 2002) and in the last years NCD has been successfully applied to different pattern recognition problems including remote sensing (Cerra et al., 2010; Cerra and Datcu, 2010).

A Content Based Image Retrieval (CBIR) system (Smeulders et al., 2000) is able to retrieve the images stored in an image database using as image indexing values the feature vectors extracted from the images by means of computer vision and digital image pro-

cessing techniques. The increasing amount of Earth Observation data provided by hyperspectral sensors, motivates research in CBIR systems capable of mining such a huge available data. There are some recent works in hyperspectral CBIR systems focused on computing the similarities between the spectral signatures of the materials in the images (endmembers) extracted by some endmember induction algorithm (Plaza et al., 2007; Veganzones et al., 2008). The NCD approach to pattern recognition is parameter-free (except for the compressor's internal parameters configuration) avoiding to tune up parameters to realize operative implementations of CBIR systems. Moreover, it does not require any feature extraction process. However, the use of NCD in a CBIR system demands a high computational cost due to the need of performing the compression of the concatenations of the query image to each of the images in the database. The use of dictionaries (Macedonas et al., 2008; Cerra and Datcu, 2010) has been proposed to provide an approximation to NCD when computational cost is an issue. Thus, we propose a CBIR system based on dictionaries for the mining of remote sensing large collections of hyperspectral images. We compare the use of dictionaries to the use of NCD in three datasets of real hyperspectral images. Results validate the pro-

posed dictionary-based hyperspectral CBIR system.

The paper is divided as follows: Sections 2 and 3 briefly review the NCD and the dictionary distances, FDD and NDD, respectively. Section 4 introduces the proposed Dictionary-based hyperspectral CBIR system. Section 5 presents the experimental methodology. Section 6 gives the results. Finally, we present some conclusions and further work in Section 7.

2 NORMALIZED COMPRESSION DISTANCE

The *conditional Kolmogorov complexity* of a signal x given a signal y , $K(x|y)$, is the length of the shortest program running in an universal Turing machine, that outputs x when fed with input y . The *Kolmogorov complexity* of x , $K(x)$, is the length of the shortest program that outputs x when fed with the empty signal λ , that is, $K(x) = K(x|\lambda)$. The *information distance*, $E(x, y)$, is an universal metric distance defined as the length of the shortest binary program in a Turing sense that, from input x outputs y , and from input y outputs x . It is formulated as:

$$E(x, y) = \max \{K(x|y), K(y|x)\}. \quad (1)$$

The *normalized information distance*, $NID(x, y)$, is defined as:

$$NID(x, y) = \frac{E(x, y)}{\max \{K(x), K(y)\}}. \quad (2)$$

The NID is sometimes known as the *similarity metric* due to its universality property. Here, universality means that for every admissible distance $D(x, y)$, the NID is minimal, $E(x, y) \leq D(x, y)$, up to an additive constant depending on D but not on x and y . However, $NID(x, y)$ relies on the notion of Kolmogorov complexity which is non-computable in the Turing sense.

The *normalized compression distance*, $NCD(x, y)$, is a computable version of (2) based on a given compressor, C . It is defined as:

$$NCD(x, y) = \frac{C(xy) - \min \{C(x), C(y)\}}{\max \{C(x), C(y)\}} \quad (3)$$

where $C(\cdot)$ is the length of a compressed signal by using compressor C , and xy is the signal resulting of the concatenation of signals x and y . If the compressor C is normal, then the NCD is a quasi-universal similarity metric. In the limit case when $C(\cdot) = K(\cdot)$, the $NCD(x, y)$ becomes "universal". The $NCD(x, y)$ differs from the ideal $NID(x, y)$ -based theory in three

aspects (Cilibrasi and Vitanyi, 2005): (a) The universality of $NID(x, y)$ holds only for indefinitely long sequences x, y . When dealing with sequences of finite length n , universality holds only for normalized admissible distances computable by programs whose length is logarithmic in n . (b) The Kolmogorov complexity is not computable, and it is impossible to know the degree of approximation of $NCD(x, y)$ with respect to $NID(x, y)$. (c) To calculate the $NCD(x, y)$ a standard lossless compressor C is used. Although better compression implies a better approximation to Kolmogorov complexity, this may not be true for $NCD(x, y)$. A better compressor may not improve compression for all items in the same proportion. Experiments show that differences are not significant if the inner requirements of the underlying compressor C are not violated.

3 DICTIONARY DISTANCES

The use of NCD (3) for CBIR entails an unaffordably cost due to the requirement of compressing the concatenated signals, $C(xy)$. To deal with this problem, we propose the use of distances based on the codewords of the dictionaries extracted by means of dictionary-based compressors, such as the LZW for text strings. This dictionary approach only requires set operations to calculate the distance between two signals given that the dictionaries have been previously extracted. Thus, dictionary distances are suitable for mining large image databases where the dictionaries of the images in the database can be extracted off-line.

Given a signal x , a dictionary-based compression algorithm looks for patterns in the input sequence from signal x . These patterns, called *words*, are subsequences of the incoming sequence. The compression algorithm result is a set of unique words called *dictionary*. The dictionary extracted from a signal x is hereafter denoted as $D(x)$, with $D(\lambda) = \emptyset$ only if λ is the empty signal. The union and intersection of the dictionaries extracted from signals x and y are denoted as $D(x \cup y)$ and $D(x \cap y)$ respectively. The dictionaries satisfy the following properties (correspondent proofs can be found in (Macedonas et al., 2008)):

1. Idempotency: $D(x \cup x) = D(x)$.
2. Monotonicity: $D(x \cup y) \geq D(x)$.
3. Symmetry: $D(x \cup y) = D(y \cup x)$.
4. Distributivity: $D(x \cup y) + D(z) \leq D(x \cup z) + D(y \cup z)$.

We have found two dictionary distance functions on the literature, the Normalized Dictionary Distance

(NDD) (Macedonas et al., 2008) and the Fast Dictionary Distance (FDD) (Cerra and Datcu, 2010):

$$NDD(x, y) = \frac{D(x \cup y) - \min\{D(x), D(y)\}}{\max\{D(x), D(y)\}}, \quad (4)$$

$$FDD(x, y) = \frac{D(x) - D(x \cap y)}{D(x)}. \quad (5)$$

NDD and FDD are both normalized admissible distances satisfying the metric inequalities. Thus, they result in a non-negative number in the interval $[0, 1]$, being zero when the compared files are equal and increasing up to one as the files are more dissimilar.

4 HYPERSPECTRAL CBIR BY DICTIONARIES

Figure 1 shows the Hyperspectral CBIR system scheme based on dictionaries. The core of the CBIR system is the dictionary distance between two hyperspectral images by means of their previously extracted dictionaries. The system interacts with a dictionary database where the images dictionaries are stored. These dictionaries have been previously extracted by off-line application of a dictionary-based compression algorithm. System interrogation is done using a query example approach. Firstly, the query example is processed to extract its dictionary and secondly, it is compared to the images in the database using the dictionary distance. A ranking of the images in the database is elaborated by ascending order of dissimilarity (ascending distance) to the query. Finally, the system returns the k images in the database corresponding to the first k ranking positions, where k is known as the query's *scope*.

5 EXPERIMENTAL METHODOLOGY

5.1 Datasets

The hyperspectral HyMAP data was made available from HyVista Corp. and German Aerospace Center's (DLR) optical Airborne Remote Sensing and Calibration Facility service¹. The sensed scene corresponds to the radiance captured by the sensor in a flight line over the facilities of the DLR center in Oberpfaffenhofen (Germany) and its surroundings, mostly fields,

¹<http://www.OpAiRS.aero>

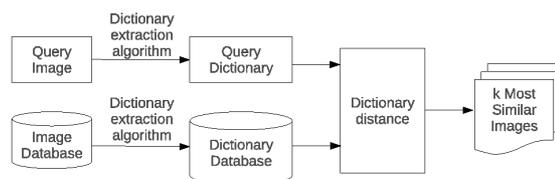


Figure 1: Hyperspectral CBIR based on dictionary schema.

forests and small towns. Figure 2 shows the scene captured by the HyMAP sensor. The data cube has 2878 lines, 512 samples and 125 bands; and the pixel values are represented by 2-bytes signed integers.

We cut the scene in patches of 64×64 pixels size for a total of 360 patches forming the hyperspectral database used in the experiments. We grouped the patches by visual inspection in five rough categories. The three main categories are 'Forests', 'Fields' and 'Urban Areas', representing patches that mostly belong to one of this categories. A 'Mixed' category was defined for those patches that presented more than one of the three main categories, being not any of them dominant. Finally, we defined a fifth category, 'Others', for those patches that didn't represent any of the above or that were not easily categorized by visual inspection. The number of patches per category are: (1) Forests: 39, (2) Fields: 160, (3) Urban Areas: 24, (4) Mixed: 102, and (5) Others: 35.

We defined three datasets to validate the use of the proposed Spectral-Spatial CBIR system in a real life scenario. In the first dataset we included the patches belonging to the three main categories: Forests, Fields and Urban Areas. In second dataset we add patches from the fourth category: Mixed. Finally, third dataset contains the patches from all five categories.

5.2 CBIR Performance Measures

Evaluation metrics from information retrieval field have been adopted to evaluate CBIR systems quality. The two most used evaluation measures are *precision* and *recall* (Smeulders et al., 2000; Daschiel and Datcu, 2005). Precision, p , is the fraction of the returned images that are relevant to the query. Recall, q , is the fraction of returned relevant images respect to the total number of relevant images in the database according to *a priori* knowledge. If we denote T the set of returned images and R the set of all the images relevant to the query, then

$$p = \frac{|T \cap R|}{|T|} \quad (6)$$

$$r = \frac{|T \cap R|}{|R|} \quad (7)$$



Figure 2: Hyperspectral scene by HyMAP sensor capturing the DLR facilities in Oberpfaffenhofen and its surroundings.

Precision and recall follow inverse trends when considered as functions of the scope of the query. Precision falls while recall increases as the scope increases. To evaluate the overall performance of a CBIR system, the Average Precision and Average Recall are calculated over all the query images in the database. For a query of scope k , these are defined as:

$$P_k = \frac{1}{N} \sum_{\alpha=1}^N P_k(H_\alpha) \quad (8)$$

and

$$R_k = \frac{1}{N} \sum_{\alpha=1}^N R_k(H_\alpha). \quad (9)$$

The Normalized Rank (Muller et al., 2001) is a performance measure used to summarize system performance into a scalar value. The normalized rank for a given image ranking Ω_α , denoted as $\text{Rank}(H_\alpha)$, is defined as:

$$\text{Rank}(H_\alpha) = \frac{1}{NN_\alpha} \left(\sum_{i=1}^{N_\alpha} \Omega_\alpha^i - \frac{N_\alpha(N_\alpha - 1)}{2} \right), \quad (10)$$

where N is the number of images in the dataset, N_α is the number of relevant images for the query H_α , and Ω_α^i is the rank at which the i -th image is retrieved. This measure is 0 for perfect performance, and approaches 1 as performance worsens, being 0.5 equivalent to a random retrieval. The average normalized rank, ANR , for the full dataset is given by:

$$ANR = \frac{1}{N} \sum_{\alpha=1}^N \text{Rank}(H_\alpha). \quad (11)$$

5.3 Methodology

We independently test the NCD (3), the NDD (4) and the FDD (5) in three experiments corresponding to each of the three previously defined datasets. Each hyperspectral image is first converted to a text file in two ways: pixel-wise and band-wise. Given that a image in a dataset is 64×64 pixels size and has 125 bands, in the pixel-wise ordering the text file is built concatenating the pixels of the images in a zig-zag way, where a pixel is a 125-components vector. In the band-wise ordering the text file is built concatenating the bands of the image, where a band is re-ordered in zig-zag to form a 64^2 -components vector. The NDD and FDD are calculated using the dictionaries extracted by the LZW compression algorithm. The NCD is calculated by CompLearn² software using default options, that is BZLIB compressor.

For each hyperspectral image H_α in a dataset we calculate the dissimilarity measure between H_α and

²<http://www.complearn.org>

each of the remaining images in the dataset using a selected distance. These dissimilarities are represented as a vector $\mathbf{s}_\alpha = [s_{\alpha 1}, \dots, s_{\alpha N}]$, where N is the number of images in the dataset and $s_{\alpha, \beta}$ is the dissimilarity between the images H_α and H_β , with $\alpha, \beta = 1, \dots, N$. We can define the ranking of the dataset relative to the query image, $\Omega_\alpha = [\omega_{\alpha, p} \in \{1, \dots, N\}; p = 1, \dots, N]$, as the set of image indexes ordered according to increasing values of their corresponding entries in the dissimilarity vector \mathbf{s}_α . That is, we sort in increasing order the components of \mathbf{s}_α , and the corresponding rendering of image indexes constitute Ω_α , so that $s_{\alpha, \omega_{\alpha, p}} \leq s_{\alpha, \omega_{\alpha, p+1}}$.

Finally, we estimate the CBIR system performance measures, average precision, average recall and average normalized rank, as follows. For each hyperspectral image H_α , a query $Q_k(H_\alpha)$ is formulated returning the k most similar (less dissimilar) images H_β in the dataset relative to the image H_α , where k is the scope of the query and takes values in the range $1 \leq k \leq N$. The groundtruth for a query image H_α is a ranking, Ω_α^{GT} , given by the a-priori categorization made by visual inspection. Given a query $Q_k(H_\alpha)$, the set of returned images $T_k(H_\alpha)$ and the set of relevant images $V_k(H_\alpha)$ are defined as follows:

$$T_k(H_\alpha) = \Omega_{\alpha, k} = [\omega_{\alpha, p} \text{ s.t. } s_{\alpha, \omega_{\alpha, p}} \leq s_{\alpha, \omega_{\alpha, k}}] \quad (12)$$

$$V_k(H_\alpha) = \Omega_\alpha^{GT} = [\beta \text{ s.t. } C(\beta) = C(\alpha)] \quad (13)$$

where $C(\gamma)$ indicates the category to which the patch H_γ belongs. This way, the relevant set for a query patch H_α is formed for all those patches belonging to its same category $C(\alpha)$. Now $T_k(H_\alpha)$ and $V_k(H_\alpha)$ can be used to calculate the average precision and recall measures of the system, as well as the average normalized rank.

6 RESULTS

Figures 3-5 show the precision-recall curves for experiments 1, 2 and 3 respectively. In each figure six precision-recall curves are drawn, corresponding to the three compared distances, NDD, FDD and NCD, applied to the datasets converted into text strings using pixel-wise and band-wise orderings. In all the experiments NDD outperforms the other distances independently of the image to text string conversion ordering used. NCD outperforms FDD showing that the lack of a normalization factor in the FDD is an important issue, affecting the performance of the retrieval system. Furthermore, we expected the band-wise ordering to perform better than the pixel-wise

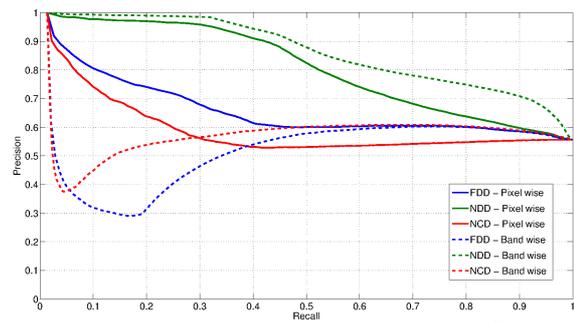


Figure 3: Precision-recall curves for HyMAP experiment 1.

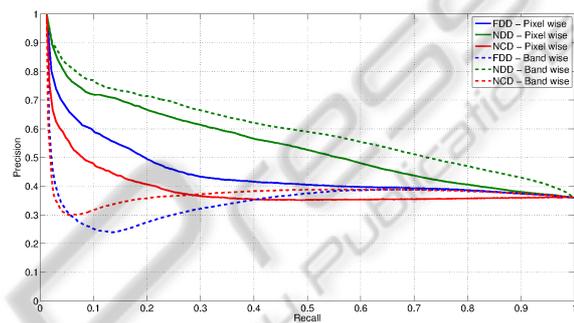


Figure 4: Precision-recall curves for HyMAP experiment 2.

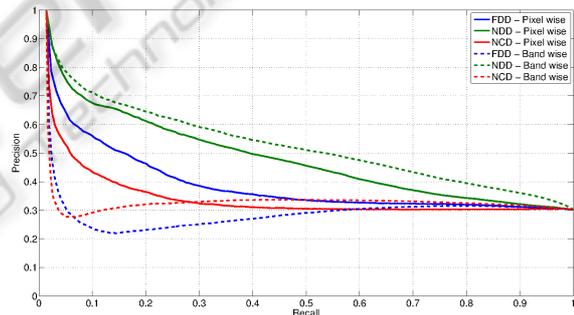


Figure 5: Precision-recall curves for HyMAP experiment 3.

ordering due to the high correlation on consecutive bands. Accordingly, the band-wise NDD gives the best performance in all the experiments. However, surprisingly, the band-wise ordering shows a bad performance for low recall values using FDD and NCD, improving as the recall values increase up to performances similar to the pixel-wise ordering. In general, the performance decreases smoothly as we include hardest categories, 'Mixed' category in experiment 2 and 'Others' category in experiment 3, yielding still good precision-recall values for the NDD function. Also, NCD presents a general lower precision compare to dictionary-based distances, although its performance decreases more slowly than the performances of NDD and FDD as we add more difficult categories.

Tables 1-3 show the Average Normalized Rank (ANR) for the experiments 1, 2 and 3 respectively. ANR results confirms the average outperform of NDD over FDD and NCD, although FDD slightly outperforms NDD in some cases. Interestingly, ANR can partially explain the effect in the FDD and NCD precision-recall curves using band-wise ordering for low recall values, as it shows FDD is having problems retrieving the 'Fields' category and NCD is having problems retrieving the 'Forests' and 'Urban Areas' categories. Further experiments must be conducted to give a better explanation to why band-wise ordering affects so much FDD and NCD performance.

Table 1: ANR results for HyMAP experiment 1.

| Category | ANR | | |
|----------------|--------------|--------------|-------|
| | FDD | NDD | NCD |
| Forests | 0.015 | 0.010 | 0.129 |
| Fields | 0.143 | 0.090 | 0.180 |
| Urban Areas | 0.005 | 0.005 | 0.086 |
| Average | 0.055 | 0.035 | 0.132 |

(a) Pixel-wise ordering

| Category | ANR | | |
|----------------|--------------|--------------|-------|
| | FDD | NDD | NCD |
| Forests | 0.073 | 0.014 | 0.292 |
| Fields | 0.159 | 0.038 | 0.118 |
| Urban Areas | 0.004 | 0.004 | 0.668 |
| Average | 0.079 | 0.019 | 0.359 |

(b) Band-wise ordering

Table 2: ANR results for HyMAP experiment 2.

| Category | ANR | | |
|----------------|--------------|--------------|-------|
| | FDD | NDD | NCD |
| Forests | 0.069 | 0.053 | 0.168 |
| Fields | 0.283 | 0.210 | 0.299 |
| Urban Areas | 0.011 | 0.012 | 0.108 |
| Mixed | 0.223 | 0.236 | 0.311 |
| Average | 0.146 | 0.128 | 0.222 |

(a) Pixel-wise ordering

| Category | ANR | | |
|----------------|--------------|--------------|-------|
| | FDD | NDD | NCD |
| Forests | 0.130 | 0.064 | 0.310 |
| Fields | 0.316 | 0.142 | 0.219 |
| Urban Areas | 0.005 | 0.006 | 0.681 |
| Mixed | 0.219 | 0.226 | 0.359 |
| Average | 0.167 | 0.109 | 0.392 |

(b) Band-wise ordering

7 CONCLUSIONS

We have introduced a Content-Based Image Retrieval System for hyperspectral databases using dictionaries. The use of a parameter-free approach based on

Table 3: ANR results for HyMAP experiment 3.

| Category | ANR | | |
|----------------|--------------|--------------|-------|
| | FDD | NDD | NCD |
| Forests | 0.065 | 0.049 | 0.162 |
| Fields | 0.323 | 0.235 | 0.315 |
| Urban Areas | 0.011 | 0.013 | 0.107 |
| Mixed | 0.246 | 0.254 | 0.318 |
| Others | 0.197 | 0.232 | 0.425 |
| Average | 0.169 | 0.156 | 0.266 |

(a) Pixel-wise ordering

| Category | ANR | | |
|----------------|--------------|--------------|-------|
| | FDD | NDD | NCD |
| Forests | 0.130 | 0.061 | 0.304 |
| Fields | 0.369 | 0.164 | 0.226 |
| Urban Areas | 0.006 | 0.008 | 0.674 |
| Mixed | 0.254 | 0.250 | 0.360 |
| Others | 0.177 | 0.210 | 0.570 |
| Average | 0.187 | 0.139 | 0.427 |

(b) Band-wise ordering

the Normalized Compression Distance (NCD) is not possible due to the computational cost of comprising the query image together to each of every image in the database. The dictionaries approach solves the computational cost problem by approximating NCD using dictionaries extracted offline from each of the database images. Results using real hyperspectral datasets show that the Normalized Dictionary Distance (NDD) outperforms the Fast Dictionary Distance (FDD) and the NCD. We also show that in order to extract the dictionaries (or compress the signals for the NCD) the arrangement of the image data in the conversion of the image to a text file affects severely the performance of the FDD and NCD similarity functions. Further experiments must be conducted to find an explanation of that unexpected effect. Generally, we can conclude that the presented results validate the use of dictionaries for hyperspectral image retrieval.

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