

Computational tools for the electronic structure study of singlet fission

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Multi-Exciton state

SF precursor

Multi-excitonic singlet as two coupled triplets ${}^1\text{ME} \sim {}^1\text{TT}$

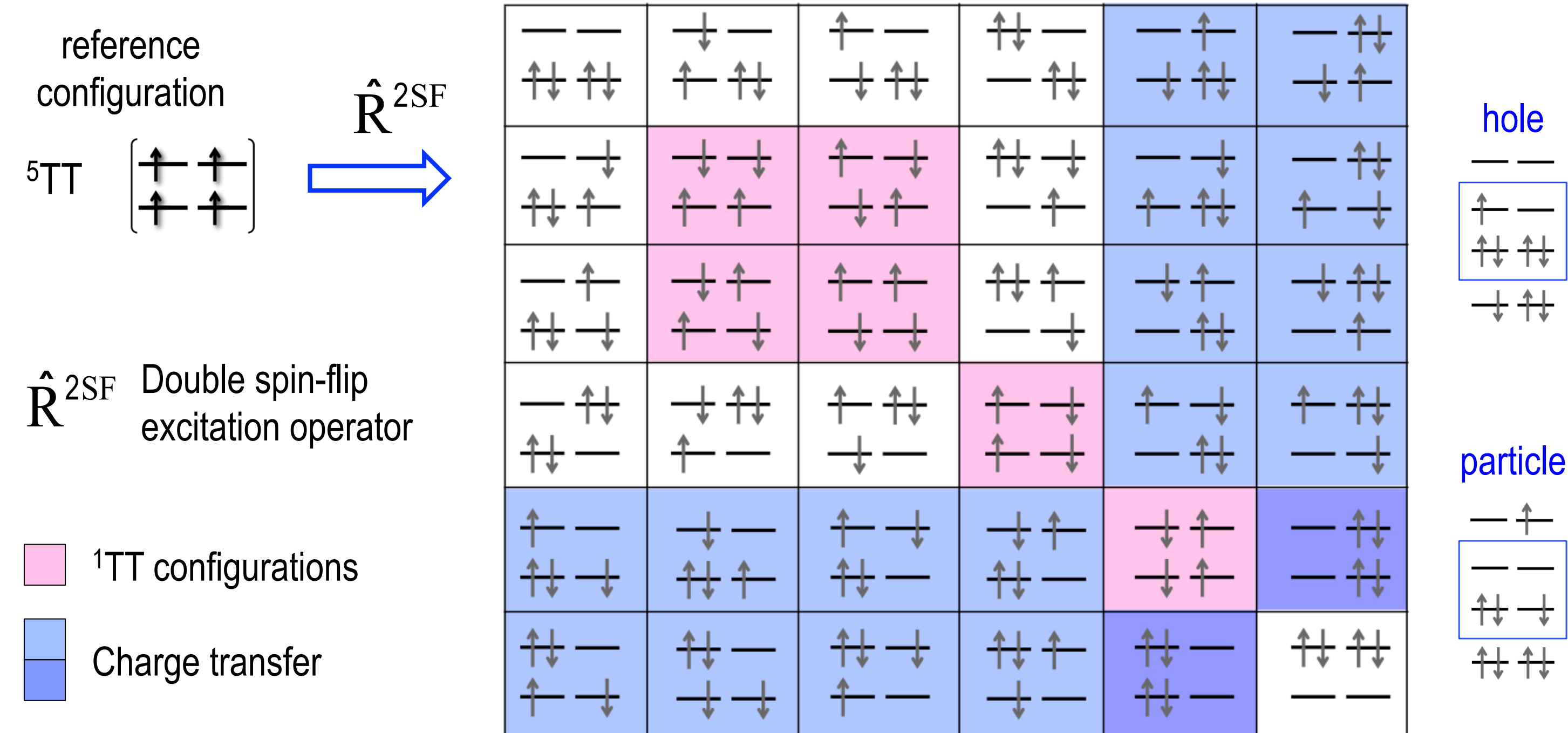
$${}^1\text{TT} = \left(\begin{array}{c} \uparrow\downarrow \\ \uparrow\downarrow \end{array} \right) + \left(\begin{array}{c} \downarrow\uparrow \\ \downarrow\uparrow \end{array} \right) + \frac{1}{2} \left(\begin{array}{c} \uparrow\uparrow \\ \downarrow\downarrow \end{array} + \begin{array}{c} \downarrow\downarrow \\ \uparrow\uparrow \end{array} \right)$$

T_1T_{-1} $T_{-1}T_1$ T_0T_0

- ${}^1\text{TT}$ states require multiple configurations
- Other configurations might be important for the adiabatic (${}^1\text{ME}$) SF precursor

RAS-2SF wavefunction

Casanova, Head-Gordon, PCCP 2009 11 9779



The RAS-2SF structure contains single-exciton, multi-exciton and charge transfer configurations

Single-Exciton states

States

- Exciton resonances
- Charge resonances
- Charge transfer
- Excimers / Trap states

Time-Dependent Density Functional Theory TDDFT

- Long-range corrected for charge separation (TDDFT)
- Dispersion corrections for weak interactions (DFT/TDDFT)

Constrain Density Functional Theory C-DFT

- DFT calculations with spin/charge constrains
- Energy of CT (diabatic) states

Fission ${}^1\text{ME} \longrightarrow T_1 + T_1$

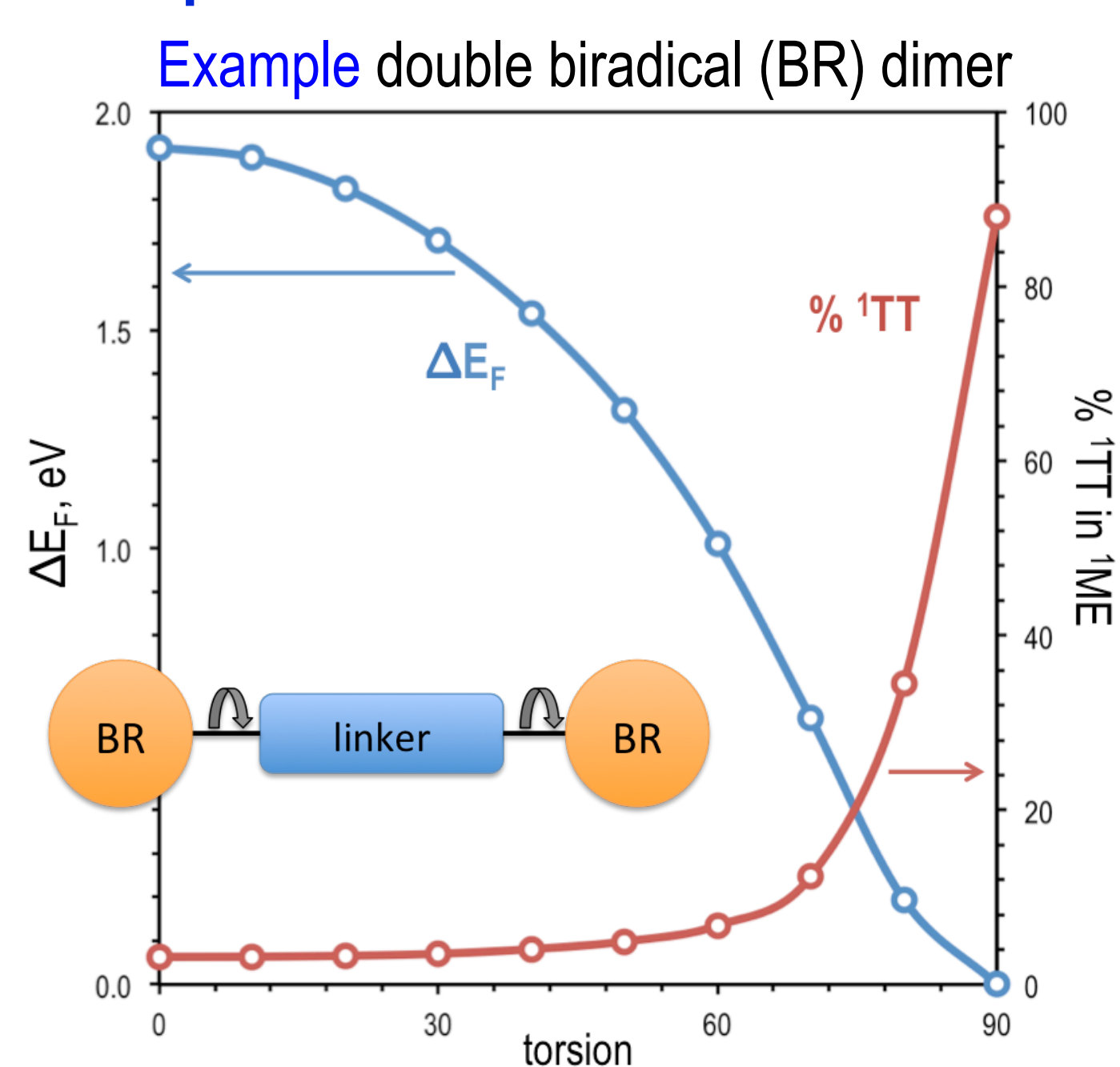
Indicators availability of the fission channel

Energy gap $\Delta E_F = E[{}^6\text{ME}] - E[{}^1\text{ME}] \rightarrow 0$ ✓

% ${}^1\text{TT}$
Contribution of ${}^1\text{TT}$ in the overall ${}^1\text{ME}$ wavefunction $\frac{[{}^1\text{TT}]}{[{}^1\text{ME}]} \rightarrow 100\%$ ✓

Radical character

Number of unpaired electrons of ${}^1\text{ME}$ $N_U = \sum_i |1 - n_i|$ $N_U \rightarrow 4$ ✓



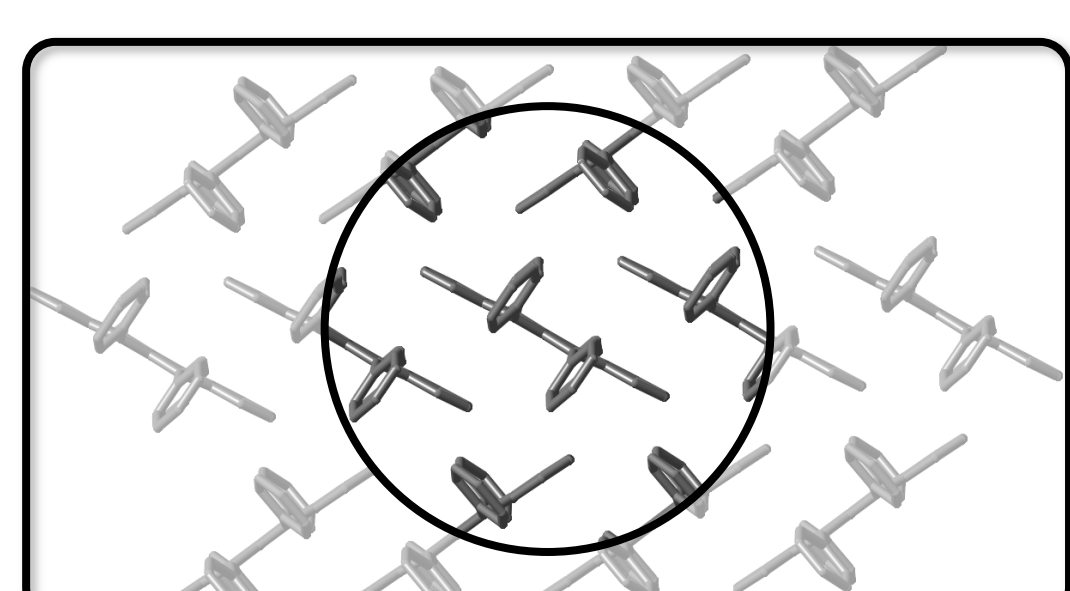
Delocalization

Dependence of transition energy with number of molecules (molecular crystal)

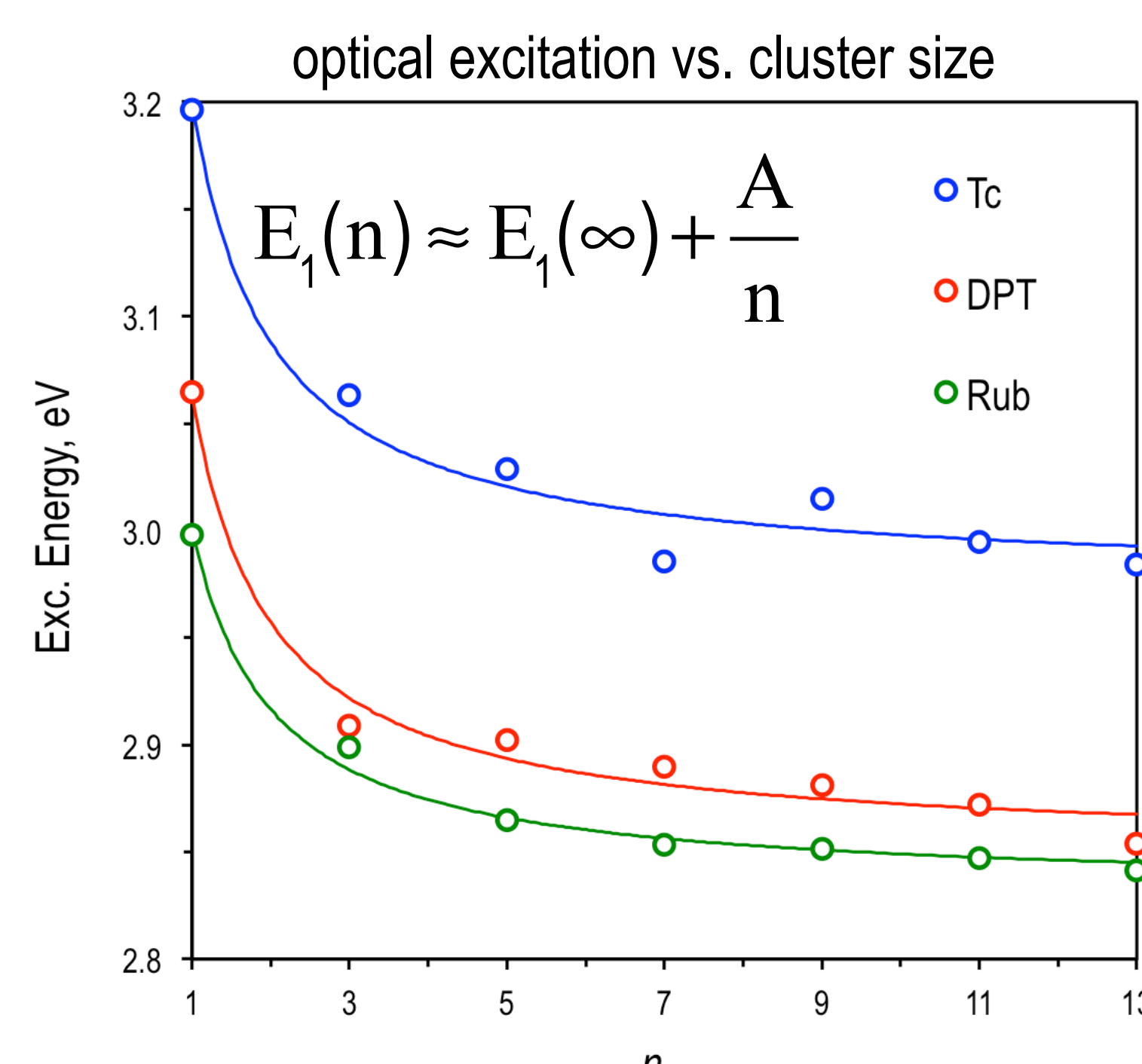
n # molecules A $\Delta E/\text{molecule}$

$E_1(\infty)$ transition crystal

$T_c > \text{DPT} > \text{Rub}$
+ coupling -



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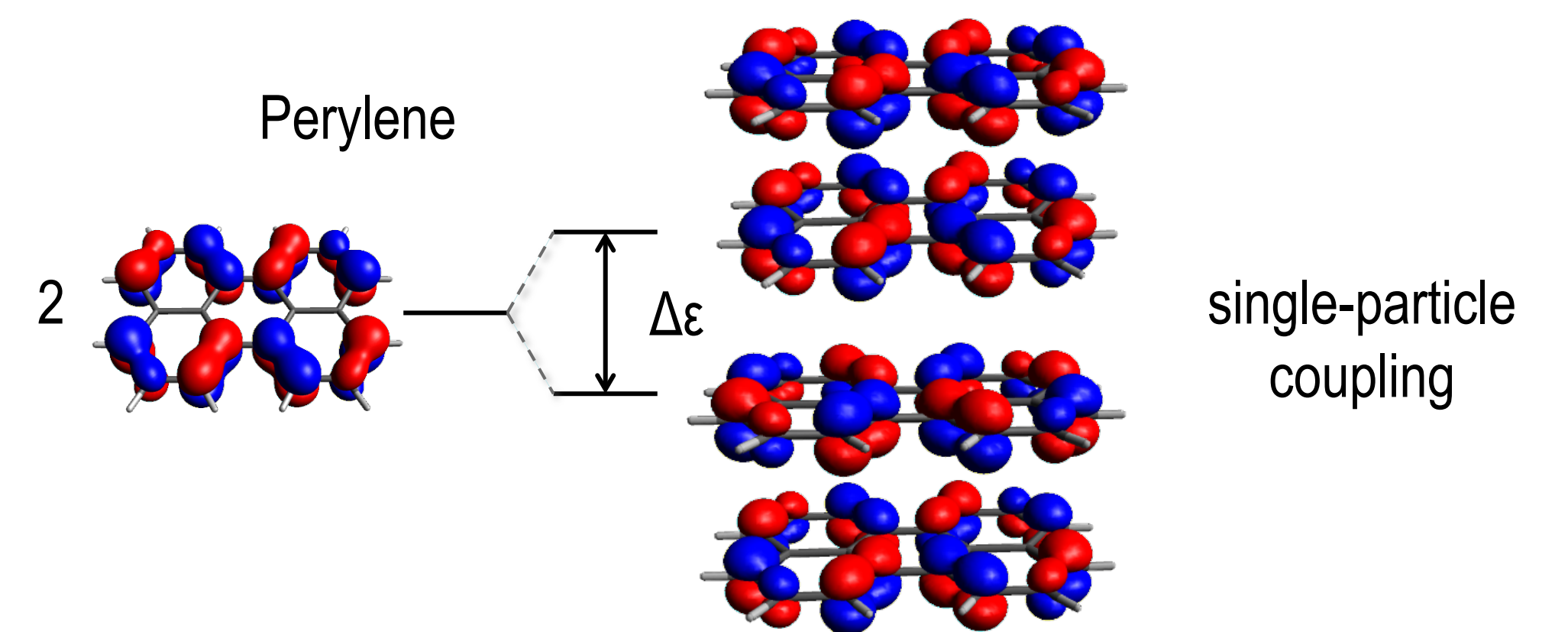


Chromophore Coupling

Orbital Splitting

$$\Delta E_H = \epsilon_{\text{HOMO}} - \epsilon_{\text{HOMO}-1}$$

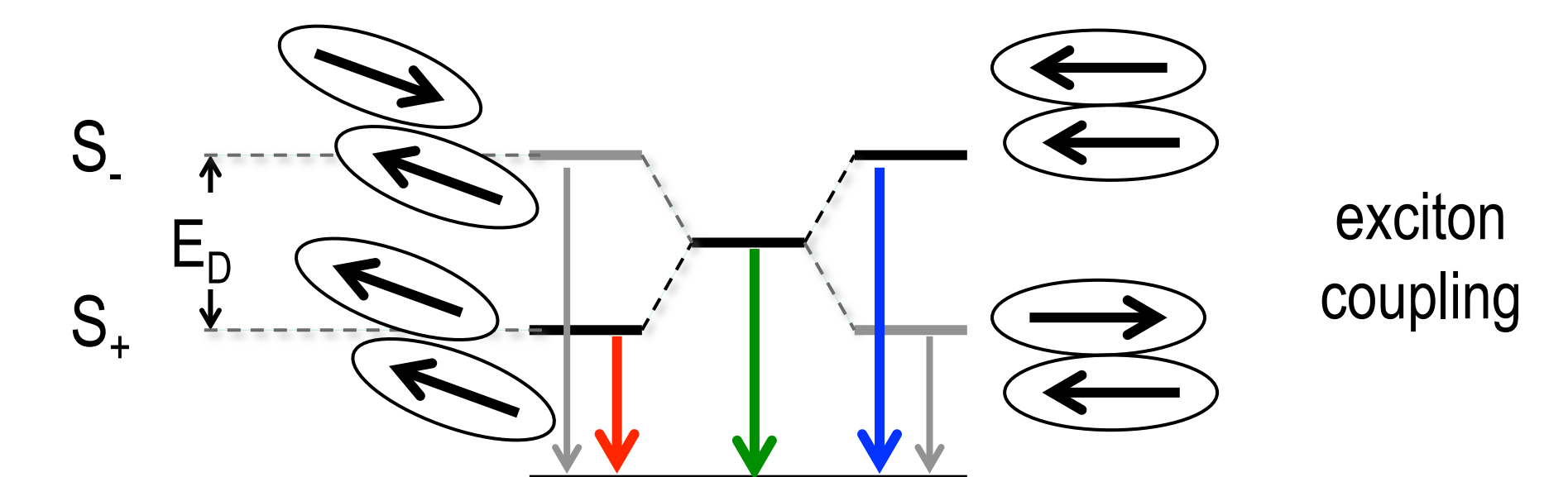
$$\Delta E_L = \epsilon_{\text{LUMO}+1} - \epsilon_{\text{LUMO}}$$



Davydov Splitting

$$S_{\pm} = \frac{1}{\sqrt{2}}(S_0 S_1 \pm S_1 S_0)$$

$$E_D = |E[S_+] - E[S_-]|$$



Diabatization

First Order

Second Order

$$\langle S_0 S_1 | \hat{H} | \text{TT} \rangle = \sum_{X \neq \text{TT}, S_0 S_1} \frac{\langle S_0 S_1 | \hat{H} | X \rangle \langle X | \hat{H} | \text{TT} \rangle}{\Delta E_X}$$

direct coupling

mediated coupling

- physically sound and intuitive
- definition diabatic states is arbitrary

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One-Particle Transition Density Matrix

Non adiabatic coupling (NAC) $\langle S_1 | \nabla_Q | {}^1\text{ME} \rangle$

$$\text{NAC} = \left| \text{Tr}[\gamma \nabla_Q] \right| \leq \|\gamma\| \cdot \|\nabla_Q\| \quad \|\gamma\|^2 = \text{Tr}[\gamma \gamma^+]$$

✗ $0 \leq \|\gamma\| \leq 1$ ✓

- magnitude of one-electron transition
- approximation to the strength of NAC

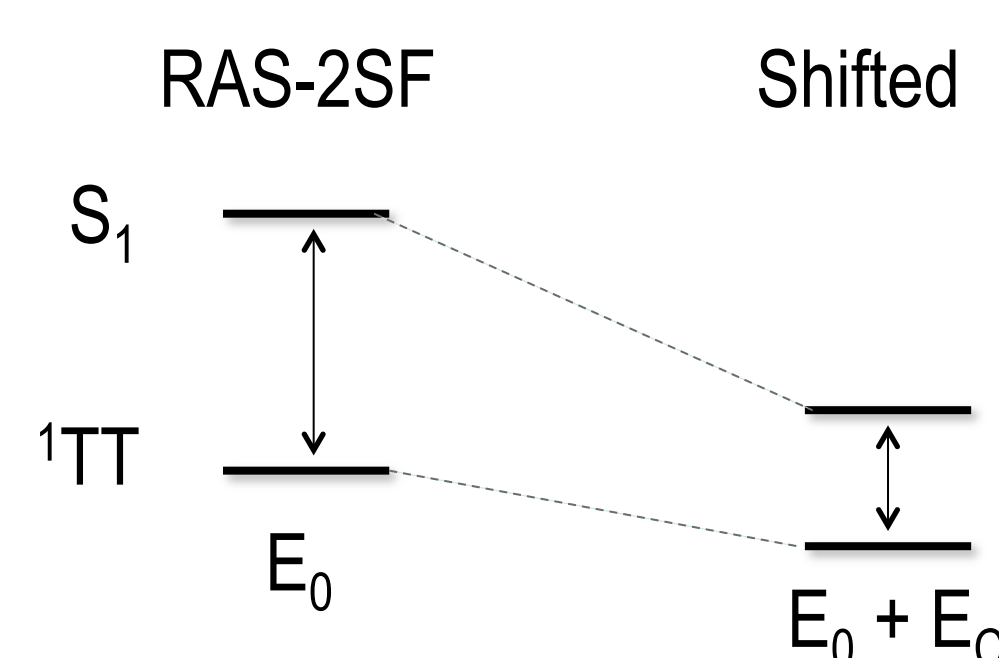
Feng, Luzanov, Krylov, J. Phys. Chem. Lett. 2013 4 3845

Dynamic correlation

RAS-2SF lack of dynamic correlation

Overestimation S_1 vs. ${}^1\text{TT}$

Energy shift



Approaches to E_R

Experimental

- Correlation + environment
- Only characterized systems

Calculations

- S_1 and T_1 monomer states
- DFT and/or *ab initio*
- Known and unknown systems

E_0 RAS-2SF energy

E_C correction energy $E_C[S_1] = E_R[S_1] - E_0[S_1]$

E_R reference energy $E_C[{}^1\text{TT}] = 2(E_R[T_1] - E_0[T_1])$

Second-order perturbation theory RAS(2)-2SF

Correction to the RAS-2SF energies

Under development



$$E^{\text{RAS}(2)} = E^{\text{RAS}} - \sum_{k \neq \text{H,P}} \frac{\langle k | \hat{H} | 0 \rangle^2}{E_k - E_0}$$

Casanova, J. Chem. Phys. 2014 140 144111